# Analysis of atmospheric pollution by quantitative infrared thermography

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#### **Abstract**

The radiation emitted by a cloud of particles depends on a lot of parameters: d, the particle diameter,  $\lambda$  the wavelength, the cloud dimensions and the complex refractive index. The presence of a functional grouping of a pollutant is characterized by an absorption band whose wavelength is always in the infrared range. We have carried out a quantitative analysis of the factors governing the monochromatic emission of radiation from a cloud. The concentration, dimensions and shape of the cloud are far less significant that the particle size. For a water cloud the contrast between two wavelengths can thus vary from -20% to -40% according to the type of cloud, and for an oil cloud from +10% to +50%. The comparison of two intensity levels obtained with a spectrophotometer , the first one in this range and the second one as a reference value, allows us to determine the presence/absence of a pollutant within the cloud of identical particles.

#### Nomenclature

T droplet temperature d droplet diameter a droplet ray n droplet complex refractive index

K Boltzman constant c light velocity h Planck constant

Q Mie efficiency factor C concentration Greek symbols  $\lambda$  wavelength  $\epsilon$  emissivity  $\alpha$  size parameter  $\Theta$  scattering angle

σ cross section

Subscripts abs absorption diff scattering ext extinction

## 1. Introduction

Our aim in this paper is to prove that the passive remote detection of pollutants is possible. Therefore, we have carried out in our laboratory a software computing the infrared thermal emission of liquid droplets clouds. The radiance level of a given cloud depends on its chemical composition. That 's the reason why we have purposed to compare the monochromatic thermal emission of two clouds containing two differents compounds (water and SF 98) for two wavelengths well chosen. A comparison of the contrast values for the water cloud and unknown cloud allows to determine if this unknown cloud contains SF 98.

A NICOLET 60 SX scans the thermal emission of the cloud in the near to far infrared range. The spectrums intensity level allows to compute the bispectral contrast at 9.7 and 12  $\mu$ m and shows a good agreement with the theory.

#### 2. Theory

#### 2.1. Thermal emission

The Planck function relates the emitted monochromatic intensity with the frequency and the temperature of an emitting medium and is expressed by :

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$$L_{\lambda}(T) = \varepsilon_{\lambda} L_{\lambda}^{0}(T) = \varepsilon_{\lambda} \frac{2 h c^{2}}{\lambda^{5} (\exp(\frac{hc}{K\lambda T}) - 1)}$$

QIRT 92 - Eurotherm Series 27 - EETI ed., Paris 1992.

 $arepsilon_{\lambda}$  defines the monochromatic emissivity of the medium and  $L^0_{\lambda}(T)$  the black body Planck thermal emission law. In our case the medium is under the form of liquid droplets. Assuming that the droplets sizes are quite larger than the wavelength and are in thermodynamic equilibrium we may write the Kirchhoff law :

$$\varepsilon_{\lambda} = Q_{abs}$$

 $Q_{abs}[1]$  represents the efficiency factor of absorption of the Mie theory, this parameter will be explicited later.

## 2.2. The Mie light scattering theory [2][6][7]

Mie has resolved the scattering of a plane wave by a homogeneous sphere. We stand here its main parameters.

Assuming that the amplitude of the incident wave is normalized to unity, the scattering intensity is given by :

$$1 (\theta) = \frac{\lambda^2}{4 \pi^2 r^2} \frac{(i_1 + i_2)}{2}$$

r represents the distance between the scattering particle and the observation point .  $i_1$  and  $i_2$  are called the intensity functions for the perpendicular and parallel components respectively.

$$i_{1} = |S_{1}|^{2}, \text{ with : } S_{1}(\theta) = \sum_{n=1}^{\infty} \frac{2 \, n + 1}{n \, (\, n + 1\, )} \left[ \, a_{n} \, \pi_{n} \, (\, \cos \theta \, ) + b_{n} \, \tau_{n} \, (\, \cos \theta \, ) \, \right]$$

$$i_2 = |S_2|^2$$
 , with :  $S_2(\theta) = \sum_{n=1}^{\infty} \frac{2n+1}{n(n+1)} [b_n \pi_n(\cos\theta) + a_n \tau_n(\cos\theta)]$ 

Note that the intensity functions depends on the the complex index of refraction , and the particle size parameter  $\alpha = 2\pi a / \lambda$ .

The efficiency factors of scattering  $Q_{diff}$ , absorption  $Q_{abs}$ , extinction  $Q_{ext}$  define some global coefficients describing the efficiencies of the scattering absorption and extinction of the incident wave in the whole solid angle  $(4\pi)$ .

$$Q_{diff} = \frac{2}{\alpha^2} \sum_{p=1}^{\infty} (|a_p|^2 + |b_p|^2)$$

$$\sigma_{ext} = \frac{\lambda^2}{\pi} \{ \text{Re}[S(0)] \} \text{ et } Q_{ext} = \frac{\sigma_{ext}}{\pi a^2}$$

$$Q_{abs} = Q_{ext} - Q_{diff}$$

Note that the efficiency factors of absorption scattering and extinction are a function of the complex refractive index and the size parameter it means the particle size.

#### 2.3. A pattern for cloud radiation emission

The FORTRAN software computes the radiation emission emerging from a spherical cloud. Our program [3] consists of:

- the cloud is discretized in cubic parts involving the totality of the physical informations inside the cloud : droplets sizes distribution, number of particles per m3, water or SF 98 liquid content;
  - the Mie parameters are weighted by the size distribution in each cubic part ;

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- one cubic part is supposed to be one particle with the averaged coefficients computed in the precedent step, and emitting isotropically towards cloud surface;
  - the decrease of the radiant intensity traversing the cloud is computed for each cubic part;
- the total thermal emission of the cloud results from the summation of each radiant intensity emerging from each cubic part.

## 3. Detection of pollutants [4]

## 3.1. Contrast at two wavelengths - definition

On using the monochromatic thermal emission values emerging out of the cloud , one can compute the contrast  $\gamma$  defined by :

$$\gamma_c = \frac{L_{\lambda_1, T_v} - L_{\lambda_2, T_v}}{L_{\lambda_1, T_v} + L_{\lambda_2, T_v}}$$

$$\gamma_{c} = \frac{Q_{abs}(n_{1},\alpha_{1}).L^{0}_{\lambda_{1},T_{v}}e^{-\beta ext(n_{1},\alpha_{1})z} - Q_{abs}(n_{2},\alpha_{2}).L^{0}_{\lambda_{2},T_{v}}e^{-\beta ext(n_{2},\alpha_{2})z}}{Q_{abs}(n_{1},\alpha_{1}).L^{0}_{\lambda_{1},T_{v}}e^{-\beta ext(n_{1},\alpha_{1})z} + Q_{abs}(n_{2},\alpha_{2}).L^{0}_{\lambda_{2},T_{v}}e^{-\beta ext(n_{2},\alpha_{2})z}}$$

where :  $L^0_{\lambda,T_v}$  is the Planck blackbody thermal emission law,  $\beta_{ext}$  the extinction coefficient proportionnal to Qext referred as the Beer-Bouguer-Lambert law and  $\alpha=\pi\,d/\lambda$  the size parameter.

## 3.2. Theoritical results - choice of $\lambda_1$ and $\lambda_2$

As it is said in introduction, our study concerns water cloud and SF 98 cloud. As many organic compounds SF 98 has a typical peak of absorptivity at 9.7  $\mu$ m (1 030 cm<sup>-1</sup>). So the first wavelength  $\lambda_1$  is imposed at 9.7  $\mu$ m. To choice  $\lambda_2$  we have computed the contrast between  $\lambda_1$  and a large group of  $\lambda_2$  values in the 8 - 12  $\mu$ m range.

#### . Case of SF 98 clouds

The ETCA CEB has given us the complex refractive index of SF 98.

The parameters on wich can depend the contrast are: the droplets size, the compound liquid content, the cloud size.

Figures 1,2 and 3 show the predicted results. As we can see on the following figure, only the size distribution has a big influence on the contrast values.

#### . Comparison with a water cloud

The Querry's article [5] has given us the complex refractive index of water.

The figure 4 shows the contrast values for a water cloud containing droplets having a diameter bigger than 6 microns.

The water and SF 98 droplets diameter have been chosen in order to approach ourself as much as possible from the diameters generated in laboratory and in order to be in good agreement with the atmospheric clouds size distribution [8] [9]. In real cases the SF6 droplets sizes are around 200  $\mu$ m and the water droplets sizes are less than 40  $\mu$ m.

The figure 5 shows that the biggest contrast difference between the two compounds appear when  $\lambda_2$  is equal to 12  $\mu$ m.

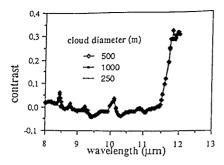


Fig.1. - Contrast around 9.7  $\mu m$  for three different clouds diameters

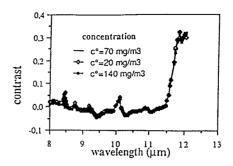


Fig.2. - Contrast around 9.7 μm for three differents liquid contents

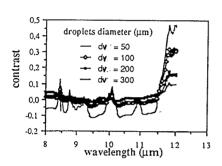


Fig.3. - Contrast around 9.7  $\mu m$  for three different droplets diameters

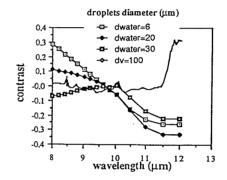


Fig.4. - Comparison between the contrast around 9.7  $\mu\text{m}$  for water and SF98

So we choose 12  $\mu m$  for  $\lambda 2$  and for our future experiments.

Note that at 9.7  $\mu$ m the complex refractive index for SF6 is n = 1.462 - i 0.2596 and n = 1 111 - i 0.008 at 12  $\mu$ m. For water n = 1.239 - i 0.045 at 9.7  $\mu$ m and n = 1.444 - i0.199 at 12  $\mu$ m.

#### . Temperature effect

The figures 5 and 6 contain curves plotting the contrast values between 9.7 and 12  $\mu m$  for each compounds.

In the two cases the contrast arises linearly with the temperature. When this one increases from 273 to 298 K the contrast given by the two clouds put 4 % up.

A  $\Delta T$  of 5 K corresponds to a  $\Delta \gamma$  of 4 %.

#### . Validation of the thermal emission

In order to valid the thermal emission pattern it is necessary to take into account the grey emittance of the earth surface and the black emittance of the sun ( $figure\ 7$ ) which is scattered by the cloud droplets. We have obtained  $10^{-4}$  -  $10^{-8}$  for the scattering intensity and thermal emission ratio. The thermal emission pattern is justified.

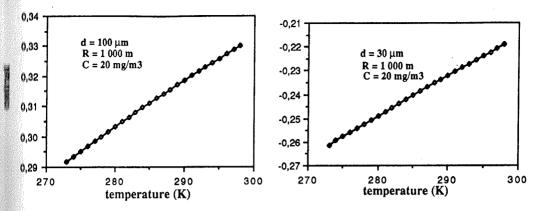


Fig.5. - Contrast around 9.7 µm against temperature for water cloud

Fig.6. - Contrast around 9.7 μm against temperature for SF98 cloud

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## 4. Experiments and results

#### 4.1. Experiments

The T.F. spectrophotometer NICOLET 60 SX allows us to realize a near to far infrared spectrums. The following scheme (*figure 8*) represents the experimental set-up mesuring the thermal emission of a liquid droplets cloud.

The HgCdTe detector owns a 10<sup>11-12</sup> detectivity (D\*). Its maximal sensivity is around 12.5 µm.

The water cloud comes out from an EVIAN spray wich generates around 40  $\mu$ m droplets. The SF6 clouds comes out from a spray sailed in the commerce and generating droplets bigger than 200  $\mu$ m.

We didn't succeed in the determination of liquid content inside the cloud.

The system parameters is the following one

- resolution: 8 cm-1
- gain: 20
- averaging on 64 consecutive spectrums

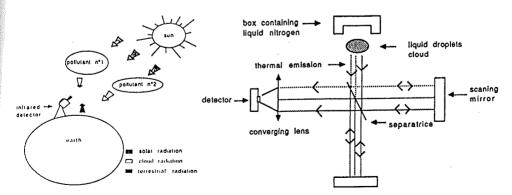


Fig.7. - Geographic context

Fig.8. - Experimental set-up

We express our gratitude to P. MASCLET (ETCA Arcueil) for doing the experiments. The first experiment consists of measure the general experimenal set-up background it means the room and the spectrophotometer (*figure 9*). Note that the intensity scale is arbitrary. In order to quantify the experiment noise and to compute the measures incertitudes we plot the two averaged spectrums ratio (*figure 10*).

The figure 9 shows that manipulation noise is constant in the 9 - 15  $\mu m$  spectral range. There is 5 % of measure incertitude for a 64 spectrums averaged spectrum. The water and SF6 spectrums are reported on figure 11.

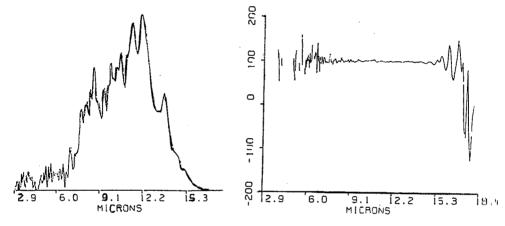


Fig.9. - Experiment background level

Fig.10. - Two averaged background spectrums ratio

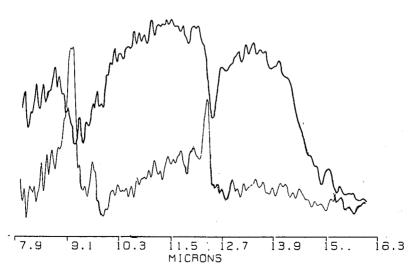


Fig.11. Water (black curve) and SF6 (grey curve) liquid droplets spectrums

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Each spectrum intensity scales were obviously the same . The following array contains the signals dynamic a and b for each wavelength 9.7 and 12  $\mu$ m (respectively) :

wavelength (micr.)	9.7	12
water	a = 6.29	b = 11.25
SF6	a = 3.87	b = 2.24

Therefore we can compute the contrast values for each cloud:

	water	SF6
contrast = (a - b)/(a + b)	- 27.8 % <sup>±</sup> 0.7 %	+ 27 % <sup>±</sup> 2 %

#### 4.2. Results

The following array resume the experimental and theoritical contrast values.

	water	SF6
diameter range (micr.)	6 to30	100 to300
theoritical contrast range	-35 % to -20 %	10 % to 30 %
experimental diameter	20 to 50	> 200
experimental contrast	- 27.8 %	+ 27 %

The contrast values between 9.7 and 12 µm seem to be in good agreement with the theory.

#### 5. Conclusion

The possibility of a passive remote detection of pollutants in the case of liquid droplets clouds has been proved. The bispectral contrast seems to be a good way for the passive remote detection if the two wavelengths are well choosen.

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